

4. (i) Workers in a certain occupancy recorded the number of children they had as follows

|   |   |    |   |   |
|---|---|----|---|---|
| 1 | 8 | 11 | 3 | 2 |
| 2 | 7 | 1  | 7 | 7 |
| 3 | 2 | 4  | 5 | 2 |
| 4 | 1 | 6  | 4 | 0 |
| 5 | 2 | 7  | 2 | 5 |

- (a) Draw a Frequency table to represent this distribution  
 (b) Find the median.  
 (c) Determine the mean.

(ii)

|                 |     |      |       |       |
|-----------------|-----|------|-------|-------|
| Number of pens  | 12  | 26   | 18    | $y$   |
| Colour          | Red | Blue | Black | Green |
| Angle of sector | 72° | $x$  | 108°  | $z$   |

The above table was used to draw a pie chart, representing colours of pens in a certain packet.

- (a) Calculate the values of  $x$ ,  $y$  and  $z$ .  
 (b) Determine the total number of pens.  
 (c) Find the probability that a pen taken out at random is either red or black.

5. (i) The position vectors of the points A and B are respectively  $4\mathbf{i} - 8\mathbf{j}$  and  $-4\mathbf{i} + \mathbf{j}$ , where  $\mathbf{i}$  and  $\mathbf{j}$  are unit vectors in the  $x$ - and  $y$ -directions respectively.

Determine

- (a)  $|\mathbf{OA}|$  (leave answer in surd form)  
 (b) the value of  $c$  given that  $\mathbf{OA}$  and  $\mathbf{OB}$  are perpendicular,  
 (c) the components of the vector  $\mathbf{BA}$ ,  
 (d) the coordinates of the point D such that  $OADB$  is a rectangle.

(ii)

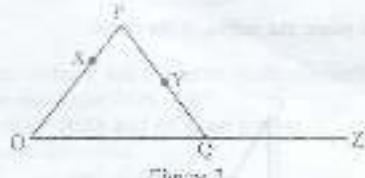


Figure 2

Figure 2 above, X is a point on  $OP$  such that  $OX : OP = 2 : 5$ , Y is the midpoint of  $OQ$ , and Z is a point on  $OQ$  produced such that  $OQ = QZ$ . Given that  $OP = p$  and  $OQ = q$ , find, in terms of  $p$  and  $q$ , the vectors

- (a)  $\mathbf{OY}$   
 (b)  $\mathbf{XY}$   
 (c)  $\mathbf{YZ}$ .

- 2
- 1.** **36.** (i) An Urban Council, in one particular year, got its revenue solely by collecting from each vehicle on the street a tax of  $\frac{1}{3}$  of its value.  
 (ii) Find the amount of tax that was paid for a car valued at £3,600 in that year.
- Of the total amount of 8.5 million francs collected by the council, 25% was used into government treasury, 15% was spent on Medical Care, 30% on Education, 10% on other needs, and the rest on Salaries.
- (b) Calculate how much was spent on Education.
- The amount spent on Education was shared between Basic and Secondary Education in the ratio 10:7.
- (c) Find the amount spent on Basic Education.  
 (d) Determine how much was spent on Salaries.  
 (e) State the mode (in lowest terms) of the amounts distributed to the two branches of expenditure.
- (iii) At the current rate 260 dollars are exchanged for 240 pounds.  
 (a) Determine the equivalent of one pound in dollars.  
 (b) Find how many dollars would be exchanged for 17,000 pounds.
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- 42.** **36.** The functions  $f$  and  $g$  are defined on  $\mathbb{R}$ , the set of real numbers, as follows:  

$$f(x) \rightarrow 3x + 2,$$

$$g(x) \rightarrow x^2 + 1.$$
- (i) Evaluate  $f(-1)$ .  
 (ii) Determine  $f^{-1}(x)$ .  
 (iii) Find the value of  $g(f(9))$ .
- (iv) Sixty students in a hostel can either play the games Monopoly ( $M$ ), Scrabble ( $S$ ) and Cards ( $C$ ). Figure 1 below shows the number of students in each region of the Venn diagram.

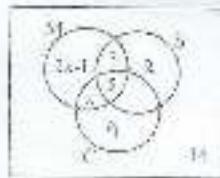


Figure 1

Given that  $n(M) = 38$ , 6 students play only cards, and that two and only two play only scrabble.

(i) determine the value of  $x$ ,  
 (ii) determine how many play only cards and scrabble,  
 (iii) find the number who play scrabble,  
 (iv) describe, in simple everyday English, the set  $C' \cap M \cap S'$ ,  
 (v) In a sketch Venn diagram, shade the region represented by  $C' \cap M \cap S'$ .

5. (i)

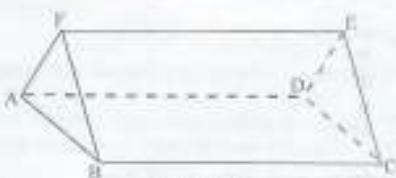


Figure 3

- (a) Determine the ratio  
faces: edges: vertices
- (b) Calculate, to two decimal places, the volume of the prism.
- (c) Find, to two significant figures, the total surface area of the prism.
- (d) The prism is melted down and cast into a solid cube. Calculate the length of the side of the cube, to one decimal place.
- (ii) The sum of the first four terms of an arithmetic progression = 16. The sum of the seventh and eighth terms is -12.  
Find the first term and the common difference of the progression.

4. (i) Use ruler, pencil and compasses only in this question.

- (a) In the middle of a fresh page, draw the line  $OX$  of length 10 cm.
- (b) Construct line  $OY$  such that  $\angle X O Y = 60^\circ$ .
- (c) Mark points  $P$  and  $Q$  on  $OX$  such that  $OP = 3$  cm and  $OQ = 7$  cm.
- (d) Construct the perpendicular bisector of  $PQ$ .
- (e) Bisect angle  $YOP$ .
- (f) Construct a circle on the chord  $PQ$  with centre  $T$  where the two bisectors in (c) and (d) intersect.

(ii)

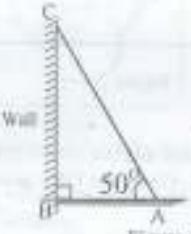


Figure 4

A ladder,  $AC$ , leaning against a vertical wall (figure 4), makes an angle of  $50^\circ$  with the floor. Given that the distance  $BA$  is 2.6 m,

Calculate, to one decimal place,

- (a) the height  $BC$
- (b) the length of the ladder  $AC$ .