UNEB U.C.E MATHEMATICS (PAPER 2) 2004

SECTION A

1. Express 784 as a product of prime factors. Hence find the square root of 784.

2. If the exchange rate of a Kenya shilling to Uganda shilling is 1 K.shs=24 Ushs. And an American dollar to Uganda shilling is \$1=ush1, 950 how many American dollars would one get in exchange for Ksh9, 750?

3. In the diagram below, BC is a tangent to the circle with centre O and angle BAO = 30.

CIRCLE

Find the size of the angles **x** and **y**.

4. Given that the representative fraction of a map is whose length on the ground is 66.25 km long.

5. The transformation described by the matrix $\begin{bmatrix} 2 & \mathbf{p} \\ \mathbf{c} & \mathbf{3} \end{bmatrix}$ maps the point **P** (-1, 3) onto its image **P''** (10, 8). Find the values of **b** and **c**.

6. In the figure below, $\overline{DE} = 8.0 \text{ cm}$, $\overline{BC} = 12.0 \text{ cm}$ and $\overline{BD} = 5.0 \text{ cm}$.

TRIANGLE

Given that \overline{DE} is parallel to \overline{BC} , find length \overline{AD} .

7. Solve the equation $3x^2 + 10x = 8$

8. Given that $133_n = 43_{ten}$, find the value of **n**.

9. A fair doe with faces marked 1, 2, 3,6 and a fair coin with one side showing a court of arms (c) and the other side a fish (F) are tossed together once.

a) Construct a possibility space showing all the possible outcomes.

b) Find the probability that a six and a fish will show up.

10. The angle of depression of the sun's rays to a man's head is 14^{0} . If the man, whose height is 1.7 m, is standing upright on horizontal ground, find the length of his shadow, correct to 2 significant figures.

SECTION B

11. a) At the beginning of the year 2000, a customer deposited shs1, 900,000 in a bank which offers a compound interest rate of 2.75% per four months. Find how much interest he earned at the end of the year.

b) a cooking oil factory offers a trade discount of 2% to its customer. It also offers a 1% cash discount to any customer who pays cash for the oil bough. If the factory price for a 20-litre jerrican of cooking oil is shs30, 000. Find the amount of money a customer saves by paying cash for 100 jerricans of the oil.

12. The coordinates of the vertices of a triangle **OAB** are **O** (0, 0), **A** (1, 0) and **B** (1, 1).

a) find the coordinates of the image formed when

(i) Triangle **OAB** undergoes a translation of $\begin{bmatrix} 2 \end{bmatrix}$ to form **O'A'B'**.

(ii) O'A'B' is transformed by the matrix $\begin{bmatrix} -2 & 0 \\ 0 & -3 \end{bmatrix}$ to form O''A''B''.

b) (i) plot triangle **OAB** and its images on the same graph.

(ii) use your graph to find the area of triangle **O''A''B''**.

13. Two cyclists C_1 and C_2 start at the same time from trading centre **P** travelling to trading centre **Q** which is 24 km apart. Cyclist C_1 starts at a steady speed of 10kmh^{-1} greater than that of cyclist C_2 who also travels at a steady speed. When C_1 has covered half the distance, he delays for three quarters of an hour, after which he travels at a speed 25% less his original speed and arrives in trading centre **Q** fifteen minutes earlier than cyclist C_2 .

a) determine the speeds of cyclists C_1 and C_2

b) If cyclist C_2 started from trading centre Q at the same time as cyclist C_1 started from trading centre P, both of them travelling non stop on the way, find how far from Q the two cyclists would meet. After how long would they meet?

14. a) Plot the graph $y = 3x^2 + 2x - 16$ of for values of $x = -3 \le x \le 3$

b) Use your graph to solve the equation $3x^2 + 2x - 8 = 0$.

15. The bearing of tower **A** from point **O** is 060° and that of tower **B** from **O**, 200° . $\overline{OA} = 24$ km and $\overline{OB} = 33$ km. Tower **C** is exactly halfway between towers **A** and **B**.

a) Using a scale of 1 cm to represent 5km, draw an accurate diagram showing the positions of the towers.

b) use your diagram to find

(i) distances \overline{AB} and \overline{OC} .

(ii)the hearing of tower **B** from tower **A**,

(iii)the bearing of tower C from O.

c) Find (i) the average speed of a cyclist who takes $2^{1/4}$ hours to travel directly from A to B

(ii) How long it takes another cyclist to travel from **A** to **B** via **O** at a steady speed of 4.5kmh⁻¹ faster than that of the cyclist in (c)(i) above.

16. The diagram below shows a quadrilateral **OSRQ.** OS = q, OP = p and SX = k (SP)

QUADRILATERAL

(i) Express vectors **SP** and **OX** in terms of **p**, **q** and **k**.

(ii) If OQ = 3p and QR = 2OS, and OX = lOR, find the values of k and l. hence find the ratio SX: XP.

17. In the diagram below VABCD is a rectangular base ABCD and V, the vertex. O is the centre of

the base **ABCD**. $\overline{AB} = 8m$. $\overline{BC} = 6m$. $\overline{VC} = \overline{VB} = \overline{VA} = \overline{VD} = 13m$. **M** is a point on **VO** such

that $\overline{3MV} = \overline{OV}$. M is also the centre of base EFGH of a small pyramid VEFGH similar to VABCD which is to be cut off from the original pyramid VABCD.

PYRAMID

Find the:

- (i) Dimensions of the base **EFGH**.
- (ii) Height of pyramid VABCD.
- (iii) Volume of the remaining part of pyramid VABCD when VEFGH is cut off.